



Syllabus

| | |
|---------------|------------------------------|
| Academic year | 2017-18 |
| Subject | 11002 - Stochastic processes |
| Group | Group 1, 1S |
| Syllabus | A |
| Language | English |

Subject

| | |
|-----------------|---|
| Name | 11002 - Stochastic processes |
| Credits | 0.75 in-class (18.75 hours) 2.25 distance (56.25 hours) 3 total (75 hours). |
| Group | Group 1, 1S (Campus Extens) |
| Period | First semester |
| Language | English |

Lecturers

| Lecturers | Office hours for students | | | | | |
|--------------------|---------------------------|----------------|----------|------------|------------|--|
| | Starting time | Finishing time | Day | Start date | End date | Office |
| | 10:00 | 11:00 | Thursday | 11/09/2017 | 15/06/2018 | IFISC, Edifici Institut Universitari de Recerca, despatx 210 |
| Pere Colet Rafecas | 10:00 | 11:00 | Tuesday | 11/09/2017 | 15/06/2018 | IFISC, Edifici Institut Universitari de Recerca, despatx 210 |

Raúl Toral Garcés
rtg803@uib.es

You need to book a date with the professor in order to attend a tutorial.

Context

This is one of the compulsory courses of the Structural Module of the master in Physics of Complex Systems. It provides a solid background on stochastic processes that will be used in other parts of the master, in particular in the course on Stochastic Simulation Methods.

Requirements

Recommended

It is recommended that the student has a basic knowledge on probability theory and statistics.

Skills



Syllabus

This course develops both specific and generic skills.

Specific

- * E2: Development and optimal application of numerical algorithms for the simulation of complex systems.
- * E6: To understand and to model processes subject to fluctuations.

Generic

- * TG1: To be able to describe, both mathematically and physically, complex systems in different situations.
- * TG2: To acquire the capacity to develop a complete research plan covering from the bibliographic research and strategy to the conclusions.
- * TG3: To write and describe rigorously the research process and present the conclusions to an expert audience.
- * TG6: To acquire high power computation skills and advanced numerical methods capabilities in applications to problems in the context of complex systems.

Basic

- * You may consult the basic competencies students will have to achieve by the end of the Master's degree at the following address: http://estudis.uib.cat/master/comp_basiques/

Content

Theme content

1. Introduction
Basic Concepts. Brownian motion. Einstein Description. Langevin description.
2. Probability
Random variables. Probability density function. Joint and conditional probabilities. Moments. Correlations. Central limit theorem. Large deviation functions. Characteristic function. Cumulants. Novikov Theorem.
3. Markov processes
Definition. Equation of Chapman-Kolmogorov. Random walk. Poisson process. Dichotomous noise. Lévy flights. Stable distributions.
4. Stochastic differential equations.
Wiener process. Continuous limit. Ito and Stratonovich interpretations. Ornstein-Uhlenbeck process.
5. Fokker-Planck equations
Derivation starting from the stochastic differential equation. Stationary solution. Potential case. Detailed balance.
6. Master equations
Birth and death processes. Stationary solutions. Approximation of Master equations by Fokker-Planck equations. Van Kampen's system size expansion.
7. Constructive effects induced by fluctuations

Syllabus

Time allowing one or two seminars will be given at the end of the course addressing some advanced topics such as: Stochastic resonance, coherence resonance and noisy precursors.

Teaching methodology

In-class work activities

| Modality | Name | Typ. Grp. | Description | Hours |
|-------------------|----------------------|-----------------|---|-------|
| Theory classes | Theoretical lectures | Large group (G) | Explanation of theoretical concepts and selected examples by the professor. | 12 |
| Practical classes | Practical sessions | Large group (G) | Resolution by the professor of selected examples and exercises. | 5 |
| Assessment | Exam | Large group (G) | This exam is intended to evaluate the knowledge acquired by the students. It will contain theoretical questions and problems. | 1.75 |

At the beginning of the semester a schedule of the subject will be made available to students through the UIBdigital platform. The schedule shall at least include the dates when the continuing assessment tests will be conducted and the hand-in dates for the assignments. In addition, the lecturer shall inform students as to whether the subject work plan will be carried out through the schedule or through another way included in the Campus Extens platform.

Distance education work activities

| Modality | Name | Description | Hours |
|-----------------------|--|---|-------|
| Individual self-study | Assignments | The student has to solve assigned exercises and submit the solutions in a written report. | 20 |
| Individual self-study | Study and understanding theoretical concepts | This activity aims at the understanding of the theoretical concepts and techniques explained in the lectures. | 36.25 |

Specific risks and protective measures

The learning activities of this course do not entail specific health or safety risks for the students and therefore no special protective measures are needed.

Student learning assessment



Syllabus

Exam

| | |
|---------------------|---|
| Modality | Assessment |
| Technique | Objective tests (retrievable) |
| Description | This exam is intended to evaluate the knowledge acquired by the students. It will contain theoretical questions and problems. |
| Assessment criteria | Accuracy of the answers. Clarity and quality of the explanations. |

Final grade percentage: 50% with minimum grade 4

Assignments

| | |
|---------------------|--|
| Modality | Individual self-study |
| Technique | Papers and projects (retrievable) |
| Description | The student has to solve assigned exercises and submit the solutions in a written report. |
| Assessment criteria | Accuracy of the results. Clarity and quality of the explanations and interpretation of the results. Quality of the written presentation. |

Final grade percentage: 50% with minimum grade 5

Resources, bibliography and additional documentation

Basic bibliography

R. Toral and P. Colet, "Stochastic Numerical Methods", Wiley (2014)
N.G. Van Kampen, "Stochastic Processes in Physics and Chemistry", 3rd edition, North Holland (2007).

Complementary bibliography

C.W. Gardiner, "Handbook of Stochastic Methods", 3rd edition, Springer (2004).
H. Risken, "The Fokker-Planck Equation", 2nd edition 3rd printing, Springer (1996).

