



Teaching guide

Subject identification

| | |
|--------------------------|--|
| Subject | 11002 - Stochastic processes |
| Credits | 0.75 de presencials (18.75 hours) 2.25 de no presencials (56.25 hours) 3 de totals (75 hours). |
| Group | Group 1, 1S (Campus Extens) |
| Teaching period | First semester |
| Teaching language | English |

Professors

| Lecturers | Horari d'atenció als alumnes | | | | | |
|---|---|----------------|--------|------------|-------------|--------|
| | Starting time | Finishing time | Day | Start date | Finish date | Office |
| Pere Colet Rafecas | 09:00 | 10:00 | Friday | 01/09/2015 | 31/07/2016 | 210 |
| Raúl Toral Garcés rtg803@uib.es | You need to book a date with the professor in order to attend a tutorial. | | | | | |

Contextualisation

This is one of the compulsory courses of the Structural Module of the master in Physics of Complex Systems. It provides a solid background on stochastic processes that will be used in other parts of the master, in particular in the course on Stochastic Simulation Methods.

Requirements

Recommendable

It is recommended that the student has a basic knowledge on probability theory and statistics,

Skills

This course develops both specific and generic skills.

Specific

- * E2: Development and optimal application of numerical algorithms for the simulation of complex systems.
- * E6: To understand and to model processes subject to fluctuations.

Generic

- * TG1: To be able to describe, both mathematically and physically, complex systems in different situations.



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- * TG2: To acquire the capacity to develop a complete research plan covering from the bibliographic research and strategy to the conclusions.
- * TG3: To write and describe rigorously the research process and present the conclusions to an expert audience.
- * TG6: To acquire high power computation skills and advanced numerical methods capabilities in applications to problems in the context of complex systems.

Basic

- * You may consult the basic competencies students will have to achieve by the end of the Master's degree at the following address: http://estudis.uib.cat/master/comp_basiques/

Content

Theme content

1. Introduction
Basic Concepts. Brownian motion. Einstein Description. Langevin description.
2. Probability
Random variables. Probability density function. Joint and conditional probabilities. Moments. Correlations. Central limit theorem. Characteristic function. Cumulants. Novikov Theorem.
3. Markov processes
Definition. Equation of Chapman-Kolmogorov. Random walk. Poisson process. Dichotomous noise. Lévy flights.
4. Stochastic differential equations.
Wiener process. Continuous limit. Ito and Stratonovich interpretations. Orstein-Uhlenbeck process.
5. Fokker-Planck equations
Derivation starting from the stochastic differential equation. Stationary solution. Potential case. Detailed balance.
6. Master equations
Birth and death processes. Stationary solutions. Approximation of Master equations by Fokker-Planck equations. Van Kampen's system size expansion.
7. Passage times and scape times
Absorbing barriers. Adjoint Fokker-Planck equation. Decay from unstable states. Scape time from metastable states.
8. Constructive effects induced by fluctuations
This topic will be given as one or two seminars at the end of the course addressing phenomena such as: Stochastic resonance, coherence resonance and noisy precursors.

Teaching methodology

In-class work activities



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| Modality | Name | Typ. Grp. | Description | Hours |
|-------------------|----------------------|-----------------|---|-------|
| Theory classes | Theoretical lectures | Large group (G) | Explanation of theoretical concepts and selected examples by the professor. | 12 |
| Practical classes | Practical sessions | Large group (G) | Resolution of assigned exercises and public presentation by the students. | 5 |
| Assessment | Exam | Large group (G) | This exam is intended to evaluate the knowledge acquired by the students. It will contain theoretical questions and problems. | 1.75 |

At the beginning of the semester a schedule of the subject will be made available to students through the UIBdigital platform. The schedule shall at least include the dates when the continuing assessment tests will be conducted and the hand-in dates for the assignments. In addition, the lecturer shall inform students as to whether the subject work plan will be carried out through the schedule or through another way included in the Campus Extens platform.

Distance education work activities

| Modality | Name | Description | Hours |
|-----------------------|--|---|-------|
| Individual self-study | Assignments | The student has to solve assigned exercises and present the solutions in written form. | 30.5 |
| Individual self-study | Study and understanding theoretical concepts | This activity aims at the understanding of the theoretical concepts and techniques explained in the lectures. | 25.75 |

Specific risks and protective measures

The learning activities of this course do not entail specific health or safety risks for the students and therefore no special protective measures are needed.

Student learning assessment

Practical sessions

| | |
|---------------------|---|
| Modality | Practical classes |
| Technique | Papers and projects (non-retrievable) |
| Description | Resolution of assigned exercises and public presentation by the students. |
| Assessment criteria | Accuracy of the results. Clarity and quality of the explanations and interpretation of the results. Quality of the oral presentation. |

Final grade percentage: 25%



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Exam

| | |
|---------------------|---|
| Modality | Assessment |
| Technique | Objective tests (retrievable) |
| Description | This exam is intended to evaluate the knowledge acquired by the students. It will contain theoretical questions and problems. |
| Assessment criteria | Accuracy of the answers. Clarity and quality of the explanations. |

Final grade percentage: 50%

Assignments

| | |
|---------------------|--|
| Modality | Individual self-study |
| Technique | Papers and projects (retrievable) |
| Description | The student has to solve assigned exercises and present the solutions in written form. |
| Assessment criteria | Accuracy of the results. Clarity and quality of the explanations and interpretation of the results. Quality of the written presentation. |

Final grade percentage: 25%

Resources, bibliography and additional documentation

Basic bibliography

R. Toral and P. Colet, "Stochastic Numerical Methods", Wiley (2014)
N.G. Van Kampen, "Stochastic Processes in Physics and Chemistry", 3rd edition, Noth Holland, 2007.

Complementary bibliography

C.W. Gardiner, "Handbook of Stochastic Methods", 3rd edition, Springer, 2004.
H. Risken, "The Fokker-Planck Equation", 2nd edition 3rd printing, Springer 1996.

